

CH 6 Multiplying a Whole Number by a Fraction

GOAL

Use repeated addition to multiply fractions by whole numbers.

1. a) Write $4 \times \frac{3}{5}$ as a repeated addition sentence.

$$\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = \underline{\quad}$$

2. Multiply. Write your answer as a fraction and as a mixed number.

a) $7 \times \frac{2}{5} =$ _____

b) $4 \times \frac{3}{8} =$ _____

3. How much farther are 3 jumps of $\frac{2}{5}$ on a number line than 2 jumps of $\frac{3}{5}$? Explain.

4. Math class is $\frac{4}{6}$ h for three days of each school week. How many hours of math class does a student have in one week?

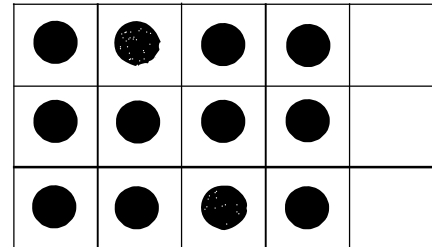
$$\underline{\quad} \times \underline{\quad} = \underline{\quad}$$

At-Home Help

To multiply a whole number by a fraction, you can:

Multiply using grids and counters.

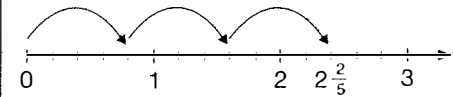
$3 \times \frac{4}{5}$ means the same as 3 sets of $\frac{4}{5}$.



Each square represents $\frac{1}{5}$, so the 12 squares covered with counters represent $\frac{12}{5}$.

Multiply using a number line.

Calculate $3 \times \frac{4}{5}$ using a number line. Write the product both as an improper fraction and as a whole or mixed number.



$$\begin{aligned} 3 \times \frac{4}{5} &= 3 \times 4 \text{ fifths} \\ &= 12 \text{ fifths} \\ &= \frac{12}{5} \text{ or } 2 \frac{2}{5} \end{aligned}$$

CH 6

Exploring Calculating a Fraction of a Fraction

GOAL

Represent one fraction as part of another fraction.

1. Draw a picture to show $\frac{1}{3}$ of $\frac{1}{4}$.
2. Determine the missing fraction. Use the fraction strip tower to help you.

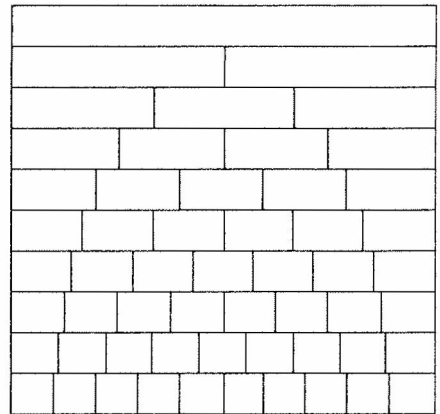
a) $\frac{1}{3}$ of $\frac{1}{2}$ is

b) $\frac{3}{4}$ of $\frac{1}{2}$ is

d) $\frac{2}{3}$ of $\frac{1}{4}$ is

At-Home Help

This fraction strip tower shows the relationship between fractions as parts of a whole.



CH 6 Multiplying Fractions

GOAL

Multiply two fractions less than 1.

1. Draw a model to determine the product of $\frac{4}{5} \times \frac{1}{2}$.

2. Match each expression with its product in the box to the right.

a) $\frac{3}{4} \times \frac{2}{5}$

b) $\frac{3}{5} \times \frac{2}{3}$

c) $\frac{1}{6} \times \frac{2}{5}$

d) $\frac{3}{8} \times \frac{4}{9}$

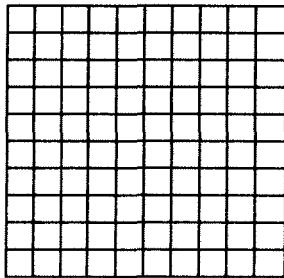
i) $\frac{2}{5}$

ii) $\frac{1}{15}$

iii) $\frac{3}{10}$

iv) $\frac{1}{6}$

3. a) Shade the grid to show why $\frac{2}{3} \times \frac{5}{8} = \frac{10}{24}$.

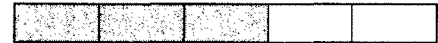


At-Home Help

To multiply $\frac{2}{3} \times \frac{3}{5}$, you can:

Use a fraction strip model.

Model $\frac{3}{5}$ and divide each fifth into thirds.



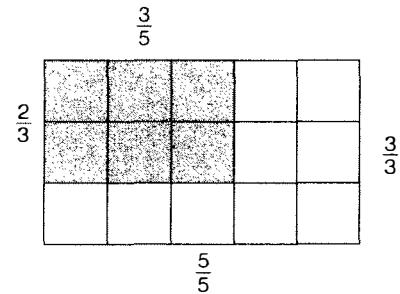
Then, to show $\frac{2}{3}$ of each section, colour 2 of the thirds.



$$\frac{2}{3} \times \frac{3}{5} = \frac{6}{15}$$

Use a grid model.

Calculate the area of a rectangle $\frac{2}{5}$ of a unit wide and $\frac{2}{3}$ of a unit long.



The coloured rectangle has $2 \times 3 = 6$ squares, so its area is $\frac{6}{15}$ square units.

$$\frac{2}{3} \times \frac{3}{5} = \frac{6}{15}$$

Multiply.

You can multiply the numerators and the denominators. For example,

$$\frac{2}{3} \times \frac{3}{5} = \frac{2 \times 3}{3 \times 5} \text{ or } \frac{6}{15}$$

CH 6 Exploring Estimating Fraction Products

GOAL

Solve the following fraction multiplication questions

a) $\frac{5}{3} \times \frac{4}{5}$

b) $\frac{6}{7} \times \frac{9}{10}$

c) $\frac{2}{3} \times \frac{4}{5}$

d) $\frac{4}{9} \times \frac{7}{13}$

At-Home | Help

Top x Top
Bottom x Bottom

Change to mixed number and
reduce when necessary

$$\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

2.

a) $\frac{1}{9} \times \frac{1}{2}$

b) $\frac{1}{1000} \times \frac{1}{100}$

c) $\frac{10}{20} \times \frac{7}{14}$

d) $\frac{5}{7} \times \frac{8}{9}$

a) $\frac{5}{11} \times \frac{7}{15}$

b) $\frac{8}{9} \times \frac{7}{8}$

c) $\frac{4}{9} \times \frac{3}{7}$

d) $\frac{2}{3} \times \frac{3}{6}$

CH 6

Multiplying Fractions Greater than 1

GOAL

Multiply mixed numbers and improper fractions.

Solve

1. ~~Estimate~~ each product.

a) $1\frac{1}{3} \times 1\frac{2}{3}$

b) $3\frac{1}{5} \times 6\frac{3}{8}$

2. Multiply the following

a) $1\frac{1}{2} \times 1\frac{1}{3} =$ _____

b) $3\frac{1}{5} \times 2\frac{1}{4} =$ _____

3. Multiply using improper fractions.

a) $2\frac{1}{5} \times 3\frac{1}{6} =$ _____ \times _____ or _____

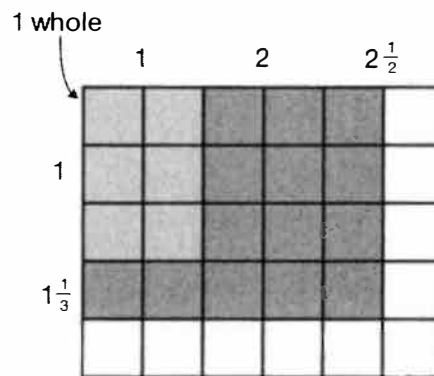
b) $2\frac{1}{4} \times 3\frac{1}{3} =$ _____ \times _____ or _____

At-Home Help

To multiply mixed fractions, you can:

Use an area model.

For example, to calculate the area of a rectangle $1\frac{1}{3}$ units long and $2\frac{1}{2}$ units wide:



$$1\frac{1}{3} \times 2\frac{1}{2} = \frac{20}{6} \text{ or } \frac{4}{3} \times \frac{5}{2} = \frac{20}{6}$$

There are 6 squares in a whole, so each square is $\frac{1}{6}$. There are 20 squares in the coloured rectangle.

Another way to record this is $1 + 1 + \frac{8}{6} = 2\frac{8}{6}$, or $3\frac{2}{6}$, or $3\frac{1}{3}$

There are two wholes and 8 other squares in the coloured rectangle.

Multiply improper fractions.

Write each mixed number as an improper fraction and multiply as you would with proper fractions.

$$\begin{aligned} 1\frac{1}{3} \times 2\frac{1}{2} &= \frac{4}{3} \times \frac{5}{2} \\ &= \frac{4 \times 5}{3 \times 2} \\ &= \frac{20}{6} \end{aligned}$$

CH 6 Dividing Fractions by Whole Numbers

GOAL

Solve these division questions

1. $\frac{6}{9} \div 4 =$

2. a) $\frac{2}{3} \div 5$

3. Divide.

a) $\frac{5}{3} \div 10 =$ _____
 = _____

b) $\frac{2}{7} \div 4 =$ _____
 = _____

4. $\frac{4}{5}$ of a room has to be painted. 3 painters are going to share the job. What fraction of the room will each painter complete if they all paint at the same rate?

At-Home Help

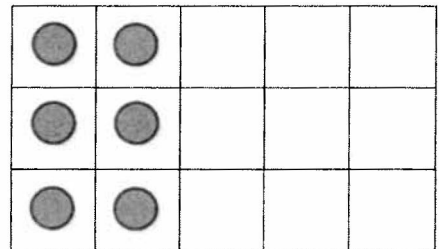
To divide a fraction by a whole number, you can:

Think of it as sharing.

For example, $\frac{2}{5} \div 3$ tells you the share size if 3 people share $\frac{2}{5}$ of something.

You cannot share $\frac{2}{5}$ equally among three people, so write an equivalent fraction.

$$\frac{2}{5} = \frac{6}{15}$$



$\frac{3}{15}$ are in each group,
 so $\frac{2}{5} \div 3 = \frac{2}{15}$.

Multiply by a fraction.

For example, $\frac{2}{5} \div 3$ is the same as $\frac{1}{3}$ of $\frac{2}{5}$, or $\frac{1}{3} \times \frac{2}{5} = \frac{2}{15}$.

Divide using an equivalent fraction, where the numerator is a multiple of the whole number.

For example, $\frac{2}{5} \div 3 = \frac{6}{15} \div 3$
 = $\frac{2}{15}$

CH 6 Estimating Fraction Quotients

GOAL

Solve these division questions

1. Estimate the quotient as a whole number.

a) $\frac{5}{10} \div \frac{3}{8}$

b) $\frac{3}{7} \div \frac{5}{9}$

2. Solve

a) $\frac{8}{10} \div \frac{1}{4}$

b) $\frac{8}{3} \div \frac{1}{2}$

c) $\frac{3}{2} \div \frac{3}{7}$

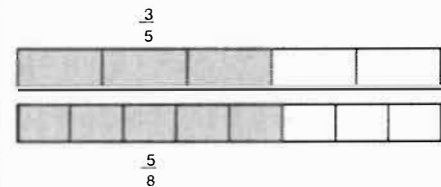
d) $\frac{1}{2} \div \frac{2}{3}$

At-Home Help

To estimate a quotient of fractions less than 1, you can:

Compare fractions by multiplying.

For example, estimate $\frac{3}{5} \div \frac{1}{8}$.

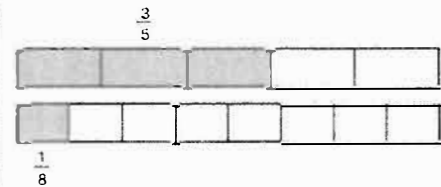


$5 \times \frac{1}{8} = \frac{5}{8}$, which is close to $\frac{3}{5}$.

$\frac{3}{5} \div \frac{1}{8}$ is close to 5.

Use fraction strips to visualize the quotient.

For example, to see how $\frac{3}{5}$ relates to $\frac{1}{8}$, see how many times $\frac{1}{8}$ fits into $\frac{3}{5}$. It looks like it fits about 5 times.



Compare using equivalent fractions.

For example, $\frac{3}{5} = \frac{24}{40}$ and $\frac{1}{8} = \frac{5}{40}$. 24 is about 5 times greater than 5, so $\frac{3}{5} \div \frac{1}{8}$ is close to 5.

CH 6 Dividing Fractions by Measuring

GOAL

Divide fractions using models and using equivalent fractions with a common denominator.

1. Calculate using common denominators.

$$\text{a) } \frac{1}{4} \div \frac{7}{8} = \frac{\square}{\square} \div \frac{7}{8}$$

$$= \underline{\hspace{2cm}}$$

$$\text{b) } \frac{3}{4} \div 2\frac{1}{2} = \frac{3}{4} \div \frac{\square}{\square}$$

$$= \underline{\hspace{2cm}}$$

2. Calculate each quotient using equivalent fractions.

$$\text{a) } 1\frac{1}{2} \div \frac{2}{3} = \frac{\square}{\square} \div \frac{\square}{\square}$$

$$= \frac{\square}{\square} \div \frac{\square}{\square}$$

$$= \underline{\hspace{2cm}}$$

$$\text{b) } \frac{2}{3} \div 1\frac{1}{2} = \frac{\square}{\square} \div \frac{\square}{\square}$$

$$= \frac{\square}{\square} \div \frac{\square}{\square}$$

$$= \underline{\hspace{2cm}}$$

3. Sally has $3\frac{1}{2}$ L of apple juice in the fridge. Each glass holds $\frac{1}{3}$ L.

- a) Set up a division statement to calculate how many glasses of apple juice Sally can pour.

$$\underline{\hspace{2cm}} \div \underline{\hspace{2cm}}$$

- b) Solve your statement. How many glasses of apple juice can Sally pour?

$$\underline{\hspace{2cm}} \div \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \div \underline{\hspace{2cm}}$$

$$= \underline{\hspace{2cm}} \div \underline{\hspace{2cm}}$$

$$= \underline{\hspace{2cm}}$$

4. Does order matter when you divide fractions? Explain.

At-Home Help

To divide two fractions, you can:

Determine the number of times the divisor fits into the dividend using fraction strips and a common denominator.

For example, to calculate $\frac{2}{3} \div \frac{4}{9}$:



Compare using equivalent fractions.



$$\frac{2}{3} \div \frac{4}{9} = \frac{6}{9} \div \frac{4}{9}$$

$$= 6 \div 4$$

$$= 1\frac{2}{4} \text{ or } 1\frac{1}{2}$$

CH6

Dividing Fractions Using a Related Multiplication

GOAL

Divide fractions using a related multiplication.

1. Calculate.

a) $\frac{2}{3} \div \frac{3}{4} = \underline{\quad} \times \underline{\quad}$ or $\underline{\quad}$

b) $\frac{4}{5} \div \frac{3}{5} = \underline{\quad} \times \underline{\quad}$ or $\underline{\quad}$

c) $\frac{5}{6} \div \frac{1}{3} = \underline{\quad} \times \underline{\quad}$ or $\underline{\quad}$

d) $\frac{7}{16} \div \frac{6}{20} = \underline{\quad} \times \underline{\quad}$ or $\underline{\quad}$

2. Write =, <, or > in each box. Calculate the quotients that are greater than 2.

a) $\frac{6}{10} \div \frac{1}{4} \square 2$; $\frac{6}{10} \div \frac{1}{4} = \underline{\quad}$

b) $\frac{1}{3} \div \frac{2}{1} \square 2$; $\frac{1}{3} \div \frac{2}{1} = \underline{\quad}$

c) $\frac{7}{8} \div \frac{2}{5} \square 2$; $\frac{7}{8} \div \frac{2}{5} = \underline{\quad}$

d) $\frac{2}{3} \div \frac{1}{2} \square 2$; $\frac{2}{3} \div \frac{1}{2} = \underline{\quad}$

3. Why does it make sense that $\frac{6}{7} \div \frac{2}{3}$ is greater than $\frac{6}{7}$?4. Jack delivers newspapers as his part-time job. It takes $5\frac{1}{2}$ min to deliver one newspaper.

a) How many newspapers can Jack deliver in 20 min? $\underline{\quad} \div 5\frac{1}{2} = \underline{\quad}$

b) How many newspapers can Jack deliver in 45 min? $\underline{\quad} \div 5\frac{1}{2} = \underline{\quad}$

c) How many newspapers can Jack deliver in $1\frac{1}{2}$ h? $\underline{\quad} \div 5\frac{1}{2} = \underline{\quad}$

At-Home Help

To divide two fractions, you can:

Multiply by the reciprocal.The reciprocal is the fraction that results from switching the numerator and denominator. For example, $\frac{4}{5}$ is the reciprocal of $\frac{5}{4}$. Calculate using the reciprocal.

$$\begin{aligned} \frac{2}{3} \div \frac{4}{9} &= \frac{2}{3} \times \frac{9}{4} \\ &= \frac{18}{12} \\ &= 1\frac{6}{12} \text{ or } 1\frac{1}{2} \end{aligned}$$

CH 6 Order of Operations

GOAL

Use the order of operations in calculations involving fractions.

1. Calculate using the rules for order of operations.

a) $\left(\frac{1}{2} + \frac{1}{3}\right) \times \frac{6}{7} =$

b) $\frac{3}{4} \div \left(\frac{1}{2} + \frac{1}{4}\right) =$

c) $\frac{4}{6} \div \left(\frac{5}{7} \div \frac{1}{2}\right) + \frac{2}{4} =$

d) $\frac{4}{6} \div \left(\frac{5}{7} \times \frac{1}{2} + \frac{2}{4}\right) =$

e) $\left(\frac{5}{10} - \frac{1}{3} \times \frac{2}{8} + \frac{1}{5}\right) \div \frac{1}{6} =$

2. Place brackets to make this equation true.

$$3 \times \frac{2}{3} + \frac{1}{3} \div \frac{1}{4} = 12$$

At-Home Help

The order of operations is:

- Perform the operations in the brackets first.
- Divide and multiply from left to right.
- Add and subtract from left to right.
- Write the answer as a mixed number.

For example:

$$\begin{aligned} \frac{3}{2} - \frac{2}{5} \div \frac{1}{5} \times \frac{3}{10} + \frac{2}{3} & \text{ Divide.} \\ = \frac{3}{2} - 2 \times \frac{3}{10} + \frac{2}{3} & \text{ Multiply.} \\ = \frac{3}{2} - \frac{6}{10} + \frac{2}{3} & \text{ Subtract.} \\ = \frac{15}{10} - \frac{6}{10} + \frac{2}{3} & \\ = \frac{9}{10} + \frac{2}{3} & \text{ Add.} \\ = \frac{27}{30} + \frac{20}{30} & \\ = \frac{47}{30} \text{ or } 1\frac{17}{30} & \end{aligned}$$